

JENSEN AND HERMITE-HADAMARD INCLUSIONS FOR STRONGLY CONCAVE SET-VALUED MAPS

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Abstract

Counterparts of the classical integral and discrete Jensen inequalities and the Hermite-Hadamard theorem and its converse, for strongly concave set-valued maps, are presented.

Keywords and phrases: strongly convex function, strongly concave set-valued map, Jensen inequality, Hermite-Hadamard inequality.

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