

## PERIODICITY IN A DELAYED KOLMOGOROV MUTUALISM MODEL ON TIME SCALES

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### Abstract

This paper is devoted to a delayed Kolmogorov mutualism model on time scales. With the help of a continuation theorem based on coincidence degree theory, we establish easily verifiable criteria for the existence of periodic solutions. Some known results are shown to be special cases of the presented paper.

**Keywords and phrases:** mutualism model, periodic solution, time scale, delay, coincidence degree.

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